

$$\sum_i q_i \wedge \dot{q}_i = \sum_i \langle q_i \wedge \dot{q}_i \rangle = 0.$$